

# Liquid-Liquid Extraction Equilibrium Data of Cobalt Nitrate–Nickel Nitrate–Nitric Acid Solutions

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Studies of the solvent extraction of cobalt and nickel nitrates from aqueous solution would add to the fundamental knowledge of extraction of metal salts. In experiments performed to determine the extractability of these metals as nitrates from aqueous solutions by organic solvents, normal butanol was found to be the best solvent and gave equilibrium distribution coefficients  $K$  for cobalt or nickel nitrate of about 0.3. The presence of nitric acid tended to decrease these at high metal concentrations.

In mixtures of the two metals the  $K$  value of either metal was found to depend on the total metal concentration. Low separation factors of about 1.3 were obtained. Very high  $K$  values of over 5 were obtained for the equilibrium extraction of the nitric acid in the presence of the metal nitrates by the  $n$ -butanol an indication of commercial possibilities.

Solvent extraction of cobalt and nickel salts from aqueous solutions has received considerable attention in recent years, partly owing to the development of many hydrometallurgical or chemical processes which are being used to separate metals in ores. The evaluation of extraction as a potential method of removing metals from aqueous solutions has been very limited by the lack of basic equilibrium data for the distribution of the metal salts between the two immiscible solvent layers.

Detailed studies on the extraction of cobalt and nickel chlorides (3), thiocyanates (5), perchlorates (4), sulfates (7), and acetates (5) are available. In the first three systems the distribution coefficients of the two metals depended on the total concentration of the anion, which was the same as the anion of the nickel and cobalt salts. High separation factors or ratios of distribution coefficients were obtained in the chloride and thiocyanate systems.

The nitrates of cobalt and nickel could easily be formed from the nitric acid leaching of ores. Study of the nitrate system should add to the fund of basic knowledge of the solvent extraction of metal salts. Hence experiments were performed on the nitrate system in this work. Templeton and Daly (10, 11) have obtained some experimental data using  $n$ -hexyl alcohol as a solvent.

In the present work the distribution coefficients of cobaltous and nickelous nitrate between water and various immiscible organic solvents were determined. Then  $n$ -butyl alcohol was selected as the best solvent, and further studies were carried out with the cobalt and nickel nitrates and various additives such as nitric acid.

## EXPERIMENTAL METHODS

Cobalt, alone in the aqueous or organic phase, was determined colorimetrically in

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a sulfuric acid solution by using the method of Gagnon (2). When the organic solvent was present, it was removed by evaporation with nitric acid. For very dilute solutions the method of Yoe (12) was used. When the ferric ion was present, it was removed by extraction with isopropyl ether. Also cupric ion, when present, was removed by precipitation as the sulfide.

In the solvent search phase, when nickel nitrate was alone in either layer, it was analyzed colorimetrically by the method

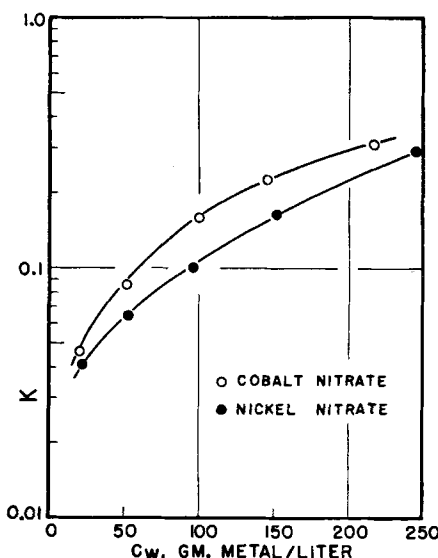


Fig. 1. Distribution coefficients in the ternary systems cobalt or nickel nitrate–water– $n$ -butanol at 25.0°C. (Cobalt or nickel equilibrated separately.)

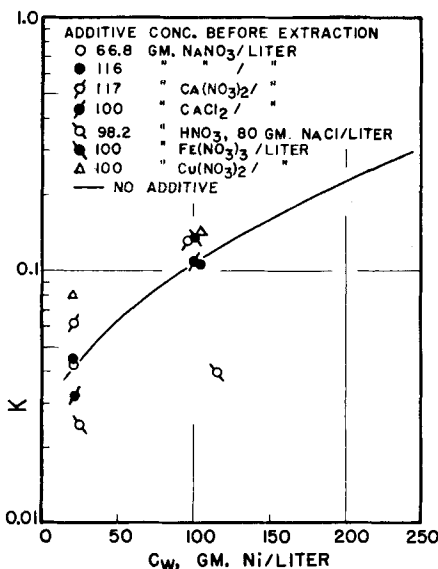


Fig. 2. Effect of additives in the system nickel nitrate–water– $n$ -butanol at 25.0°C.

TABLE 1. SOLVENT SEARCH DATA AT 25.0°C.

(Metals equilibrated separately)

| Solvent                         | Metal | $C_w$ , g./liter | $C_o$ , g./liter      |
|---------------------------------|-------|------------------|-----------------------|
| Alcohols                        |       |                  |                       |
| $n$ -Butanol                    | Ni    | 21.15            | $8.76 \times 10^{-1}$ |
| $n$ -Butanol                    | Ni    | 96.50            | 9.76                  |
| $n$ -Butanol                    | Co    | 20.70            | $9.75 \times 10^{-1}$ |
| $n$ -Butanol                    | Co    | 99.60            | 16.00                 |
| $n$ -Amyl alcohol               | Ni    | 20.30            | $3.97 \times 10^{-2}$ |
| $n$ -Amyl alcohol               | Co    | 22.00            | $6.47 \times 10^{-2}$ |
| Isoamyl alcohol                 | Ni    | 20.75            | $4.33 \times 10^{-2}$ |
| Isoamyl alcohol                 | Co    | 22.00            | $5.76 \times 10^{-2}$ |
| $n$ -Hexyl alcohol              | Ni    | 96.00            | $6.80 \times 10^{-2}$ |
| $n$ -Hexyl alcohol              | Ni    | 20.20            | $1.29 \times 10^{-2}$ |
| $n$ -Hexyl alcohol              | Co    | 21.20            | $2.15 \times 10^{-2}$ |
| Cyclohexanol                    | Co    | 21.80            | $2.80 \times 10^{-1}$ |
| 2-Octanol                       | Ni    | 20.85            | $9.78 \times 10^{-3}$ |
| $n$ -Decyl alcohol              | Ni    | 20.78            | $6.91 \times 10^{-3}$ |
| Ketones                         |       |                  |                       |
| Methyl ethyl ketone             | Ni    | 15.15            | $1.18 \times 10^{-1}$ |
| Methyl isopropyl ketone         | Co    | 22.55            | $<1.0 \times 10^{-3}$ |
| 3-Pentanone                     | Ni    | 19.38            | $2.60 \times 10^{-3}$ |
| 4-Methyl, 2-pentanone           | Ni    | 18.85            | $6.04 \times 10^{-3}$ |
| 4-Methyl, 2-pentanone           | Co    | 21.30            | $1.52 \times 10^{-3}$ |
| Diisobutyl ketone               | Ni    | 19.70            | $1.98 \times 10^{-3}$ |
| Ethers                          |       |                  |                       |
| Diethyl ether                   | Ni    | 18.18            | $8.7 \times 10^{-4}$  |
| Isopropyl ether                 | Ni    | 19.52            | $8.84 \times 10^{-4}$ |
| Isopropyl ether                 | Co    | 20.7             | $<1.0 \times 10^{-3}$ |
| Ethylene glycol monoethyl ether | Ni    | 16.35            | $1.05 \times 10^{-2}$ |
| Nitrogen Compounds              |       |                  |                       |
| 2-Nitropropane                  | Ni    | 19.60            | $6.07 \times 10^{-4}$ |
| Others                          |       |                  |                       |
| Carbon tetrachloride            | Ni    | 19.65            | $2.59 \times 10^{-4}$ |
| Benzene                         | Ni    | 19.23            | $4.66 \times 10^{-4}$ |
| Ethyl acetate                   | Ni    | 18.97            | $3.5 \times 10^{-4}$  |

of Snell and Snell (9). When *n*-butanol was the solvent, the method of Gagnon (2) in sulfuric acid solution was adopted for use with nickel. In the presence of iron, nickel was analyzed by the dimethylglyoxime gravimetric method. This was necessary, since even traces of ferric ion interfere in the colorimetric determination of nickel sulfate at 397 m $\mu$ . (6).

A colorimetric procedure was developed for the analysis of cobalt and nickel when together in sulfuric acid solution. Beer's law can be written for the peak absorbance of nickel sulfate solution at 397 m $\mu$ , another Beer's law equation can be written for the relatively weak absorbance at 518 m $\mu$ , separate equations can be written for cobalt sulfate at its peak of 518 and at 397 m $\mu$ , and these four equations can then be combined. Then the absorbance of solutions containing both metals was measured at the two peaks of 397 and 518 m $\mu$  and the concentrations calculated from the combined equations. Known mixtures were analyzed and gave an average deviation of 1.8% and a maximum of 2.8% (6).

Nitric acid was determined by using 0.2*N* sodium hydroxide and an electro-titrator. Ferric ion was analyzed by the dichromate method and copper by electro-deposition. The *n*-butyl alcohol and metal salts used were reagent grade.

Equal volumes of initial aqueous-phase solution and pure solvent were used in the equilibrium experiments. The equilibrium extractions were performed in rubber-sealed, glass-stoppered flasks agitated by magnetic stirrers and totally immersed in a bath. The densities were determined by weighing the contents from calibrated pipettes. The ternary-phase diagram was determined by titrating known amounts of one phase with another until the solution became cloudy. Experimental details are available elsewhere (6).

#### DISCUSSION OF SOLVENT SEARCH DATA

To select the best solvents distribution ratios (ratio of concentration in

organic to concentration in aqueous phase) of cobalt nitrate and nickel nitrate alone were obtained between water and a variety of solvents (Table 1) at 25.0°C. The solvents used were restricted to those known to have some ability to extract metal salts.

The ketones gave distribution ratios *K* of about 0.008 as a maximum, and the ethers gave values less than 0.001 for the cobalt and nickel nitrates. The alcohols were the best solvents with maximum *K* values of about 0.2, the *K* value decreasing with increasing solvent molecular weight. *N*-butyl alcohol was selected for further studies because of its high *K* value compared with that of other solvents. This solvent was also used in the studies of the sulfate system (7).

#### N-BUTANOL-COBALT OR NICKEL NITRATE-WATER-ADDITIVE SYSTEM

##### No Additives

Distribution data from the solvent *n*-butanol when either the cobalt or nickel is alone are given in Table 2. Figure 1 shows that the *K* for nickel or cobalt increases markedly as the concentration of the metal in the water increases. At about 250 g. metal/liter the *K* is approximately 0.3. The *K* of cobalt is slightly greater than that of nickel.

If the distribution coefficient is assumed to follow the equation

$$K' = C_o / (C_w)^n \quad (1)$$

than a log-log plot of *C<sub>o</sub>* vs. *C<sub>w</sub>* should be a straight line with slope *n*. Plots of the cobalt nitrate and nickel nitrate data give straight lines which are almost parallel with an *n* value of 1.69 for cobalt and 1.82 for nickel. The chloride data (3) give slopes of about 7 for both cobalt and nickel. The values for the nitrates

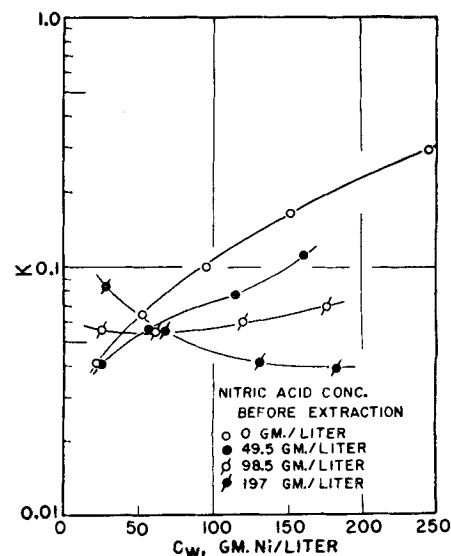


Fig. 3. Effect of nitric acid in the system nickel nitrate-water-nitric acid-*n*-butanol at 25.0°C.

TABLE 2. DISTRIBUTION OF COBALT NITRATE OR NICKEL NITRATE IN *N*-BUTANOL-WATER AT 25.0°C.

(Metals equilibrated separately)

| Water phase concentration before extraction               |                  | Water phase                  |                           | Phases at equilibrium |                              | Alcohol phase             |                   |
|---|------------------|------------------------------|---------------------------|-----------------------|------------------------------|---------------------------|-------------------|
| <i>C<sub>w</sub></i> , g./liter Metal                     | HNO <sub>3</sub> | <i>C<sub>w</sub></i> , Metal | g./liter HNO <sub>3</sub> | $\rho_w$ , g./ml.     | <i>C<sub>o</sub></i> , Metal | g./liter HNO <sub>3</sub> | $\rho_o$ , g./ml. |
| <i>N</i> -Butanol-nickel nitrate-water system             |                  |                              |                           |                       |                              |                           |                   |
| 20  | 0                | 21.15                        | 0                         |                       | 0.876                        | 0                         |                   |
| 50  | 0                | 52.5                         | 0                         |                       | 3.42                         | 0                         |                   |
| 100   | 0                | 96.5                         | 0                         |                       | 9.76                         | 0                         |                   |
| 150   | 0                | 152.2                        | 0                         | 1.350                 | 25.25                        | 0                         | 0.888             |
| 260.5*  | 0                | 244.5                        | 0                         | 1.555                 | 71.50                        | 0                         | 0.996             |
| <i>N</i> -Butanol-nickel nitrate-water-nitric acid system |                  |                              |                           |                       |                              |                           |                   |
| 150   | 197.0            | 182.5                        | 35.21                     | 1.441                 | 7.25                         | 135.2                     | 0.917             |
| 150   | 49.48            | 161.2                        | 6.87                      | 1.372                 | 17.37                        | 37.70                     | 0.889             |
| 150   | 98.5             | 175.5                        | 15.22                     | 1.402                 | 12.49                        | 71.20                     | 0.895             |
| 100   | 197.0            | 130.0                        | 60.75                     | 1.327                 | 5.46                         | 119.2                     | 0.910             |
| 100   | 49.48            | 114.2                        | 11.90                     | 1.260                 | 8.93                         | 33.45                     | 0.871             |
| 100   | 98.5             | 119.5                        | 26.72                     | 1.281                 | 7.18                         | 63.3                      | 0.883             |
| 50  | 98.5             | 61.3                         | 43.25                     | 1.156                 | 3.44                         | 52.30                     | 0.877             |
| 50  | 197.0            | 66.6                         | 91.5                      | 1.192                 | 3.73                         | 100.8                     | 0.910             |
| 50  | 49.48            | 55.2                         | 20.39                     | 1.132                 | 3.17                         | 27.05                     | 0.857             |
| 20  | 98.5             | 24.90                        | 54.5                      | 1.072                 | 1.40                         | 44.2                      | 0.876             |
| 20  | 197.0            | 27.45                        | 111.1                     | 1.101                 | 2.34                         | 90.8                      | 0.911             |
| 20  | 49.48            | 23.15                        | 28.55                     | 1.057                 | 0.948                        | 22.01                     | 0.857             |
| <i>N</i> -Butanol-cobalt nitrate-water system             |                  |                              |                           |                       |                              |                           |                   |
| 20  | 0                | 20.7                         | 0                         |                       | 0.975                        | 0                         |                   |
| 50  | 0                | 52.0                         | 0                         | 1.118                 | 4.50                         | 0                         | 0.841             |
| 105   | 0                | 99.6                         | 0                         |                       | 16.00                        | 0                         |                   |
| 150   | 0                | 145.5                        | 0                         | 1.352                 | 33.05                        | 0                         | 0.913             |
| 236*  | 0                | 217.0                        | 0                         | 1.503                 | 68.5                         | 0                         | 1.009             |
| <i>N</i> -Butanol-cobalt nitrate-water-nitric acid system |                  |                              |                           |                       |                              |                           |                   |
| 150   | 49.48            | 151.2                        | 7.52                      | 1.360                 | 21.35                        | 36.3                      | 0.906             |
| 150   | 98.5             | 167.8                        | 16.05                     | 1.387                 | 16.71                        | 70.0                      | 0.913             |
| 150   | 197.0            | 188.7                        | 37.60                     | 1.441                 | 10.35                        | 131.6                     | 0.923             |
| 100   | 49.48            | 107.9                        | 12.05                     | 1.262                 | 10.87                        | 32.7                      | 0.879             |
| 100   | 98.5             | 113.9                        | 26.68                     | 1.278                 | 9.31                         | 62.95                     | 0.890             |
| 100   | 197.0            | 122.5                        | 61.0                      | 1.319                 | 6.35                         | 117.5                     | 0.917             |
| 50  | 49.48            | 54.8                         | 20.45                     | 1.132                 | 3.88                         | 27.00                     | 0.861             |
| 50  | 98.5             | 58.7                         | 42.80                     | 1.157                 | 3.95                         | 52.20                     | 0.880             |
| 50  | 197.0            | 65.1                         | 90.80                     | 1.188                 | 4.375                        | 100.0                     | 0.910             |
| 20  | 49.48            | 23.21                        | 28.05                     | 1.057                 | 0.942                        | 21.75                     | 0.856             |
| 20  | 98.5             | 23.95                        | 55.5                      | 1.069                 | 1.645                        | 44.1                      | 0.876             |
| 20  | 197.0            | 26.80                        | 110.1                     | 1.101                 | 2.66                         | 91.0                      | 0.912             |

\*Water phase saturated with metal nitrate before extraction.

TABLE 3. DISTRIBUTION IN THE SYSTEM: *N*-BUTANOL-NICKEL NITRATE-COBALT NITRATE-WATER AT 25.0°C.

(One run made with nitric acid as an additive)

| Water phase<br>before<br>extraction |             | Phases at equilibrium |                     |           |                      |                      |                       |                       |    |                              |
|-------------------------------------|-------------|-----------------------|---------------------|-----------|----------------------|----------------------|-----------------------|-----------------------|----|------------------------------|
| $C_w'$ ,<br>Co                      | g./l.<br>Ni | Co                    | $C_w$ , g./l.<br>Ni | Co and Ni | $\rho_w$ ,<br>g./ml. | $\rho_o$ ,<br>g./ml. | Co                    | $K$                   | Ni | $\beta$ ,<br>$K_{Co}/K_{Ni}$ |
| 20                                  | 20          | 21.4                  | 21.9                | 43.3      | 1.069                | 0.8361               | $7.77 \times 10^{-2}$ | $6.30 \times 10^{-2}$ |    | 1.233                        |
| 50                                  | 50          | 47.3                  | 51.2                | 98.5      | 1.027                | 0.8641               | $1.51 \times 10^{-2}$ | $1.20 \times 10^{-1}$ |    | 1.258                        |
| 100                                 | 100         | 92.0                  | 97.7                | 189.7     | 1.445                | 0.9586               | $2.73 \times 10^{-1}$ | $2.15 \times 10^{-1}$ |    | 1.270                        |
| 100                                 | 25          | 97.3                  | 26.4                | 123.7     | 1.293                | 0.8887               | $1.84 \times 10^{-1}$ | $1.46 \times 10^{-1}$ |    | 1.260                        |
| 25                                  | 100         | 25.2                  | 99.8                | 125.0     | 1.293                | 0.8768               | $1.84 \times 10^{-1}$ | $1.44 \times 10^{-1}$ |    | 1.278                        |
| 50*                                 | 50*         | 56.1                  | 57.2                | 113.3     | 1.278                | 0.8880               | $7.78 \times 10^{-2}$ | $6.14 \times 10^{-2}$ |    | 1.266                        |

\*98.5 g. HNO<sub>3</sub>/liter before extraction.

which are near 2 might possibly be explained by dissociation of the salt in the aqueous phase. However the real significance of these  $n$  values is not yet apparent.

Runs made at different temperatures show that the  $K$  values for cobalt and nickel both decreased by approximately 30% in going from 5.5° to 69.5°C. (1) with little effect on the separation factor of  $K$  of cobalt over  $K$  of nickel. The data for the sulfates (7) show the reverse trend with the  $K$  values approximately doubling in this temperature range.

#### Additives

Data where additives were put into the *n*-butanol-metal nitrate-water system are plotted in Figure 2 for nickel (1), and the curve for no additives from Figure 1 is shown for comparison. A plot of the cobalt data gave very similar curves. The data show that the additive cupric nitrate has the largest effect, approximately doubling the  $K$  value. A mixture of nitric acid and sodium chloride decreased the  $K$ , and other additives such as calcium nitrate, calcium chloride, sodium nitrate, and ferric nitrate had little effect (1).

Since the cobalt and nickel nitrate salts would often occur in nitric acid solution, data were obtained for nitric acid as an additive; this also allows comparison with other studies where the acid counterpart of the anion of the cobalt and nickel salts was used. Figure 3 for nickel shows the effect of initial nitric acid concentration on the  $K$  value. Initial rather than equilibrium acid concentrations were used as parameters, since it is extremely difficult to control experimentally the final equilibrium acid concentrations. A similar type of plot for cobalt, which is not shown, gave the same trends as nickel. At low metal concentrations the  $K$  value increases with increasing acid concentration, but at higher metal concentrations the trend reverses and  $K$  decreases with increasing nitric acid concentration. These effects are quite different from the sulfate system, where the  $K$  of both cobalt and nickel sulfate increased a hundredfold in

going from low to high sulfuric acid concentrations. In the chloride system the  $K$  and the separation factor also increased greatly with increases in hydrochloric acid concentration.

#### Distribution Coefficient for Nitric Acid

The distribution coefficient data for nitric acid in the presence of nickel nitrate (Table 2) are plotted in Figure 4. This plot shows a very large increase in  $K$  with increasing nickel concentration in the aqueous phase with  $K$  values over 5. A similar curve is obtained when only cobalt nitrate is present, an indication of a very high extraction of nitric acid by *n*-butanol with metals present. This could be the basis for a good extraction process to recover nitric acid from aqueous salt solutions. Methods such as distillation or addition of a second solvent might then be tried to recover the acid from the *n*-butanol solvent, but further research would be needed. At zero concentration of metal the  $K$  value approaches approximately 0.7.

#### *N*-BUTANOL-COBALT NITRATE-NICKEL NITRATE-WATER SYSTEM

##### Distribution Coefficients

In Table 3 the  $K$  values are given for the complex system *n*-butanol-cobalt nitrate-nickel nitrate-water. The absolute concentrations of the cobalt and nickel were varied fivefold, and the ratio of concentration of cobalt to nickel was varied from 4 : 1 to 1 : 4. Only one run was made with nitric acid present.

In Figure 5 the  $K$  value of nickel from Table 3 is plotted vs. the total cobalt plus nickel concentration in the water at equilibrium. For comparison curves A and B from Figure 3 are shown for nickel when equilibrated in the absence of the cobalt. A similar type of plot for cobalt, which is not shown, was made, the  $K$  of

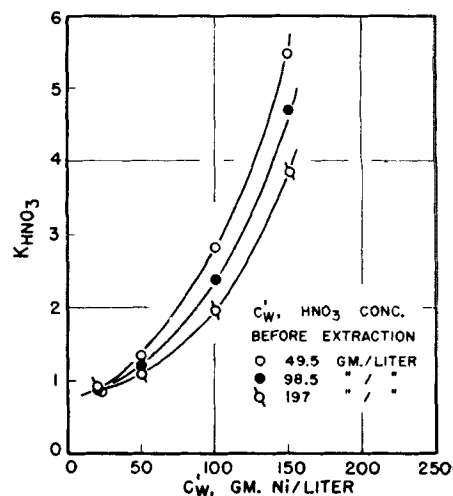


Fig. 4. Distribution coefficient of nitric acid in the system nickel nitrate-water-nitric acid-*n*-butanol at 25.0°C.

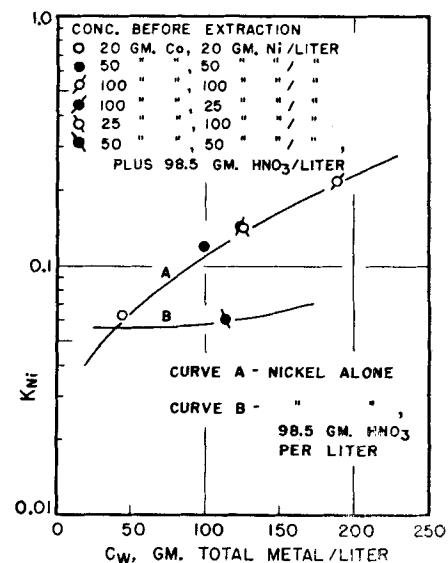


Fig. 5. Distribution coefficient of nickel nitrate in the system nickel nitrate-cobalt nitrate-water-*n*-butanol at 25.0°C.

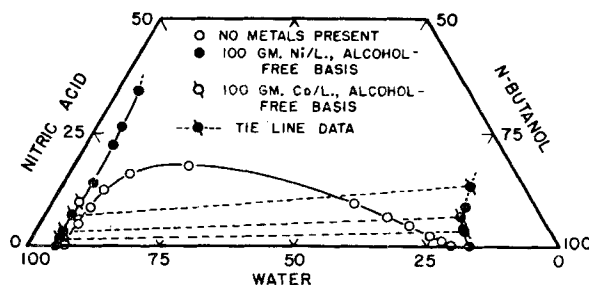


Fig. 6. Phase diagram for the system nitric acid-water-*n*-butanol at 25.0°C. (Data on a weight-percentage metal-free basis.)

cobalt being plotted vs. the total metal concentration in the water at equilibrium. This gave the same trends as nickel. That the distribution coefficient of cobalt or nickel in a mixture of the two depends only on the total metal concentration is concluded.

#### Separation Factors

When cobalt and nickel were equilibrated separately with no nitric acid present, and the initial concentration was 100 g. each metal/liter, the calculated separation factor was a maximum at 1.49. When the two metals were equilibrated together, the actual separation factor was 1.27 for the same concentrations. Hence having both metals present decreased the maximum separation factor by about 15%. These separation factors in Table 3 are all low and constant at about 1.26. The separation factor for sulfates increased slightly when the metals were equilibrated together and was between 1.2 to 1.5 depending on the sulfuric acid concentration (7). The separation factor for the chlorides increased very greatly with increases in hydrochloric acid concentration (3).

#### Phase Diagram

The phase diagram (Figure 6) is shown for the ternary system *n*-butanol-nitric acid-water on a metal-free basis; it is very similar to the *n*-butanol-sulfuric acid-water system (8). When the metal salts cobalt or nickel nitrate are present, the solubilities of the alcohol in the aqueous phase and the aqueous phase in the alcohol phase are lowered and change the phase diagram markedly (Figure 6). Densities were determined and reported in Tables 2 and 3 and elsewhere (6).

Inspection of experimental phase solu-

bility and tie line data, reported elsewhere (1) and used to plot Figure 6 show that the ratio of the nitric acid content to the water content in the phases at equilibrium are as follows. In the aqueous phase the ratio varies from 0.03 to 0.08 depending on the concentration of nitric acid. In the organic phase the ratio is about 0.2 to 0.8. Hence at equilibrium the nitric acid to water ratio is considerably higher in the organic than in the aqueous phase, and the acid is extracted preferentially by the organic solvent.

Using the triangular diagram (Figure 6) and Figures 1, 3, 4, or 5 one can predict the compositions and amounts of the two phases resulting from the equilibrium of equal volumes of an aqueous solution and the solvent. Density data can then be used to calculate relative volumes of the resultant equilibrium solutions.

#### ACKNOWLEDGMENT

Grateful acknowledgement is made to the American Cyanamid Company for their fellowships which aided in this work.

#### NOTATION

- $C$  = concentration, g. metal/liter (not g. metal salt/liter)  
 $C_0$  = equilibrium concentration of metal or nitric acid in organic phase, g./liter  
 $C_w$  = equilibrium concentration of metal or nitric acid in aqueous phase, g./liter  
 $C_w'$  = concentration of metal or nitric acid in aqueous phase before extraction, g./liter  
 $K$  = distribution coefficient,  $C_0/C_w$   
 $K'$  = distribution coefficient,  $C_0/(C_w)^n$   
 $n$  = constant

#### Greek Letters

- $\beta$  = separation factor =  $K(\text{cobalt})/K(\text{nickel})$   
 $\rho_0$  = density of organic phase at equilibrium, g./ml.  
 $\rho_w$  = density of aqueous phase at equilibrium, g./ml.

#### LITERATURE CITED

- Geankoplis, C. J., and E. J. Scharf, *Doc. 5827*, A.D.J. Auxiliary Publications Project, Washington, D. C.; \$1.25 for photoprints or 35-mm. microfilm.
- Gagnon, J., *Chemist Analyst*, No. 1, 43, 15 (1954).
- Garwin, Leo, and A. N. Hixson, *Ind. Eng. Chem.*, **41**, 2298, 2303 (1949).
- Moore, T. E., R. J. Laren, and P. C. Yates, *J. Phys. Chem.*, **59**, 90 (1955).
- Rigamonti, R., and E. Spaccemela-Marchetti, *Chim. e ind. (Milan)*, **36**, 91 (1954).
- Scharf, E. J., Ph.D. dissertation, Ohio State Univ., Columbus, Ohio (1957).
- Schlea, C. S., and C. J. Geankoplis, *Ind. Eng. Chem.*, **49**, 1056 (1957).
- Schlea, C. S., Ph.D. dissertation, Ohio State Univ., Columbus, Ohio (1955).
- Snell, F. D., and C. T. Snell, "Colorimetric Methods of Analysis," 3 ed., Vol. II, p. 346, D. Van Nostrand, New York (1948).
- Templeton, C. C., and L. K. Daly, *J. Am. Chem. Soc.*, **73**, 3989 (1951).
- , *J. Phys. Chem.*, **56**, 215 (1952).
- Yoe, J. H., "Photometric Chemical Analysis," Vol. I, p. 172, John Wiley, New York (1948).

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# Heat and Mass Transfer from Wall to Fluid in Packed Beds

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Experiments of heat and mass transfer from the tube wall to the fluids flowing through the packed beds were carried out separately. In heat transfer air was used as the fluid, and several kinds of solid particles with low and high thermal conductivities were investigated to determine effective thermal conductivities and wall heat transfer coefficients. In mass transfer the dissolution rate of the coated material on the inner wall of the packed tube to the water stream was measured, and wall mass transfer coefficients were analyzed. It was found that a close similarity exists between the  $J_H$  and  $J_D$  factor for the wall coefficients in the turbulent-flow region.

The rate of heat transfer in a packed bed is of particular interest in the process design not only of heat exchangers but also of catalytic reactors. The problem of the rate of heat transfer from the tube wall to a fluid flowing through a packed tube has been the subject of considerable study. The first work of heat transfer in a packed bed was made

by Colburn (6) in 1931. He correlated the data as the over-all heat transfer coefficients, which are similar to those for an empty tube. Thereafter several investigators (4, 12, 13) reported the correlations for over-all coefficients.

For the calculation of the temperature distributions and explanation of the mechanism of heat transfer in the bed,

the concept of the so-called "effective thermal conductivity" was introduced. Smith et. al. (21) determined values of the local effective thermal conductivity in the packed bed and found that the resistance to heat transfer increased greatly near the wall. Hatta and Maeda (15), Coberly and Marshall (5), and later workers (2, 9, 18, 19, 23) found that an additional resistance to heat transfer existed at the wall. They assumed the effective thermal conductivity to be constant within the bed and expressed the additive effect in the wall vicinity as the wall heat transfer coefficient.

This paper reports the results of both heat and mass transfer from the wall of